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SIDDHARTH INSTITUTE OF ENGINEERING & TECHNOLOGY:: PUTTUR  
(AUTONOMOUS)

B.Tech II Year I Semester Regular & Supplementary Examinations March-2023

NUMERICAL METHODS AND TRANSFORMS

(Electronics and Communication Engineering)

Time: 3 hours

Max. Marks: 60

(Answer all Five Units 5 x 12 = 60 Marks)

**UNIT-I**

- 1 a Find a positive root of the equation  $x^3 - x - 1 = 0$  by Bisection method. CO2 L3 6M  
b Apply Newton's forward interpolation formula and the given table of values CO1 L3 6M

x	1.1	1.3	1.5	1.7	1.9
f(x)	0.21	0.69	1.25	1.89	2.61

Obtain the value of f(x) when x=1.4.

OR

- 2 a Estimate a real root of the equation  $xe^x - \cos x = 0$  by using Newton-Raphson method. CO1 L4 6M  
b Use Newton's backward interpolation formula to find f(32) given f(25)=0.2707, f(30)=0.3027, f(35)=0.3386, f(40)=0.3794. CO1 L3 6M

**UNIT-II**

- 3 a Solve by Euler's method the equation  $y' = y^2 + x$ ,  $y(0)=1$  for  $y(0.1)$  and  $y(0.2)$ . CO3 L3 6M  
b Using Runge-Kutta method of fourth order, compute  $y(0.2)$  from  $y' = xy$ ,  $y(0)=1$  taking  $h=0.2$ . CO3 L3 6M

OR

- 4 Evaluate  $\int_0^1 \frac{1}{1+x} dx$  by CO3 L5 12M

(i) By Trapezoidal rule and Simpson's  $\frac{1}{3}$  rule.

(ii) Using Simpson's  $\frac{3}{8}$  rule and compare the result with actual value.

**UNIT-III**

- 5 a Find the Laplace transform of  $f(t) = \cosh at \sin bt$ . CO4 L3 6M  
b Find  $L^{-1}\left(\frac{s^2}{(s^2+4)(s^2+25)}\right)$  using Convolution theorem. CO4 L3 6M

OR

- 6 a Find the Laplace transform of  $\frac{1-\cos at}{t}$  CO4 L3 6M  
b Find  $L^{-1}\left\{s \log\left(\frac{s-1}{s+1}\right)\right\}$  CO4 L3 6M

**UNIT-IV**

- 7 a Using Laplace transform method to solve  $y' - y = t, y(0) = 1$  CO5 L3 6M  
 b Obtain the Fourier series expansion of  $f(x) = (x - x^2)$  in the interval  $[-\pi, \pi]$ . CO5 L2 6M  
 Hence show that  $\frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots = \frac{\pi^2}{12}$ .

OR

- 8 Use Laplace transform method to solve  $y'' - 3y' + 2y = 4t + e^{3t}$  where  $y(0) = 1, y'(0) = 1$  CO5 L3 12M

**UNIT-V**

- 9 a Applying Fourier integral theorem, show that  $e^{-x} \cos x = \frac{2}{\pi} \int_0^{\infty} \frac{\lambda^2 + 2}{\lambda^4 + 4} \cos \lambda x d\lambda$ . CO6 L3 6M

- b Prove that  $F[x^n f(x)] = (-i)^n \frac{d^n}{dp^n} [F(p)]$  CO6 L5 6M

OR

- 10 Find the Fourier sine and cosine transforms of  $f(x) = e^{-ax}, a > 0$  and hence deduce the integrals (i)  $\int_0^{\infty} \frac{p \sin px}{a^2 + p^2} dp$  (ii)  $\int_0^{\infty} \frac{\cos px}{a^2 + p^2} dp$  CO6 L1 12M

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